



# CLADAG 2023



BOOK OF ABSTRACTS AND SHORT PAPERS  
14th Scientific Meeting of the Classification and Data Analysis Group  
Salerno, September 11-13, 2023

edited by

Pietro Coretto  
Giuseppe Giordano  
Michele La Rocca  
Maria Lucia Parrella  
Carla Rampichini



Pearson



## SCIENTIFIC PROGRAM COMMITTEE

Carla Rampichini (chair, University of Florence - Italy)  
Claudio Agostinelli (University of Trento - Italy)  
Michela Battauz (University of Udine - Italy)  
Antonio Canale (University of Padua - Italy)  
Carlo Cavicchia (Erasmus University Rotterdam - Netherlands)  
Claudio Conversano (University of Cagliari - Italy)  
Eustasio del Barrio (University of Valladolid - Spain)  
Roberto Di Mari (University of Catania - Italy)  
Stefania Fensore (University of "G. d'Annunzio" - Italy)  
Nial Friel (University College Dublin - Ireland)  
Maria Giovanna Ranalli (University of Perugia - Italy)  
Leonardo Grilli (University of Firenze - Italy)  
Luigi Grossi (University of Padua - Italy)  
Christian Hennig (University of Bologna - Italy)  
Mia Hubert (KU Leuven - Belgium)  
Alfonso Iodice D'Enza (University of Naples "Federico II" - Italy)  
Julien Jacques (University of Lyon - France)  
José Joaquim Dias Curto (ISCTE-Instituto Universitário de Lisboa- Portugal)  
Michele La Rocca (University of Salerno - Italy)  
Silvia Montagna (University of Turin - Italy)  
Barbara Pawelek (University of Cracow - Poland)  
Fulvia Pennoni (University of Milano-Bicocca - Italy)  
Mario Rosario Guarracino (University of Cassino - Italy)  
Katrijn Van Deun (University of Tilburg - Netherlands)  
Simone Vantini (Politecnico di Milano - Italy)  
Donatella Vicari (Sapienza University of Rome - Italy)  
Helga Wagner (Johannes Kepler University Linz - Austria)  
Hiroshi Yadohisa (Doshisha University - Japan)

## LOCAL PROGRAM COMMITTEE

Michele La Rocca (chair, University of Salerno - Italy)  
Pietro Coretto (University of Salerno - Italy)  
Giuseppe Giordano (University of Salerno - Italy)  
Paolo Rocca Comite Mascambruno (University of Salerno - Italy)  
Marcella Niglio (University of Salerno - Italy)  
Maria Lucia Parrella (University of Salerno - Italy)  
Marialuisa Restaino (University of Salerno - Italy)  
Domenico Vistocco (University of Naples "Federico II" - Italy)  
Maria Prosperina Vitale (University of Salerno - Italy)

## CLADAG 2023 BOOK OF ABSTRACTS AND SHORT PAPERS:

14th Scientific Meeting of the Classification and Data Analysis Group, Salerno, September 11-13, 2023  
edited by Carla Rampichini, Michele La Rocca, Pietro Coretto, Giuseppe Giordano, Maria Lucia Parrella

Front cover: Genome sequence map, chromosome architecture and genetic sequencing chart abstract data,  
© Tartila / Shutterstock

© 2023

Published by Pearson Education Resources, Italia

[www.pearson.it](http://www.pearson.it)

ISBN: 9788891935632

# INDEX

<b>Preface</b>	<b>XVII</b>
<b>Plenary Session</b>	<b>1</b>
<i>Francesco Bartolucci, Michael Greenacre, Silvia Pandolfi and Fulvia Pennoni</i>	
<b>Discrete latent variable models: recent advances and perspectives</b>	<b>3</b>
<i>Gerda Claeskens, Sarah Pirenne, Snigdha Panigrahi and Yiling Huang</i>	
<b>Selective inference after variable selection by the randomized group Lasso method</b>	<b>7</b>
<i>Fancesca Greselin</i>	
<b>To get the best, tame the beast: robust ML estimation for mixture models</b>	<b>8</b>
<i>Thomas Kneib</i>	
<b>Rage against the mean - an introduction to distributional regression</b>	<b>12</b>
<i>Sofia Charlotta Olhede</i>	
<b>On graph limits as models for interaction data</b>	<b>13</b>
<b>Invited Papers</b>	<b>15</b>
<i>Alessandro Albano, Mariangela Sciandra and Antonella Plaia</i>	
<b>Ensemble method for text classification in medicine with multiple rare classes</b>	<b>17</b>
<i>Alessandro Albano, Mariangela Sciandra and Antonella Plaia</i>	
<b>Distance-based aggregation and consensus for preference-approvals</b>	<b>21</b>
<i>Marco Alfò, Dimitris Pavlopoulos and Roberta Varriale</i>	
<b>Flexible employment, a machine learning approach</b>	<b>25</b>
<i>Federico Ambrogi and Matteo Di Maso</i>	
<b>Clinically useful measures in survival analysis: the restricted mean survival time as an alternative to the hazard ratio</b>	<b>29</b>
<i>Jose Ameijeiras-Alonso</i>	
<b>Data-driven smoothing parameter selection for circular data analysis</b>	<b>33</b>
<i>Laura Anderlucci, Silvia Dallari and Angela Montanari</i>	
<b>View it differently: finding groups in microbiome data</b>	<b>34</b>
<i>Rabea Aschenbruck, Gero Szepannek and Adalbert F. X. Wilhelm</i>	
<b>Random-based initialization for clustering mixed-type data with the k-prototypes algorithm</b>	<b>38</b>
<i>Filippo Ascolani and Valentina Ghidini</i>	
<b>Posterior clustering for Dirichlet process mixtures of Gaussians with constant data</b>	<b>42</b>

<i>Vincent Audigier and Ndèye Niang</i>	
<b>Multiple imputation for clustering on incomplete data</b>	<b>46</b>
<i>Alejandra Avalos-Pacheco and Roberta De Vito</i>	
<b>Integrative factor models for biomedical applications</b>	<b>50</b>
<i>Silvia Bacci, Bruno Bertaccini, Carla Galluccio, Leonardo Grilli and Carla Rampichini</i>	
<b>Test equating with evolving latent ability</b>	<b>54</b>
<i>Michela Baccini, Alessandra Mattei, Elena Degli Innocenti, Giulio Biscardi and Aitana Lertxundi</i>	
<b>Causal inference on the impact of extreme ambient temperatures on population health</b>	<b>58</b>
<i>Zsuzsa Bakk</i>	
<b>Measurement invariance testing of latent class models using residual statistics and likelihood ratio test</b>	<b>61</b>
<i>Falco J. Bargagli-Stoffi, Costanza Tortù and Laura Forastiere</i>	
<b>Network interference and effect modification</b>	<b>65</b>
<i>Francesco Barile, Simonón Lunagómez and Bernardo Nipoti</i>	
<b>Flexible modelling of heterogeneous populations of networks: a Bayesian nonparametric approach</b>	<b>69</b>
<i>Mario Beraha and Jim E. Griffin</i>	
<b>Normalized latent measure factor models</b>	<b>70</b>
<i>Silvia Bianconcini and Silvia Cagnone</i>	
<b>Estimation issues in multivariate panel data</b>	<b>74</b>
<i>Alessandro Bitetto and Paola Cerchiello</i>	
<b>The nexus between ESG and initial coin offerings: evidence from text analysis</b>	<b>78</b>
<i>Laura Bocci and Donatella Vicari</i>	
<b>A clustering model for three-way asymmetric proximity data</b>	<b>82</b>
<i>Ilaria Bombelli, Ichcha Manipur and Maria Brigida Ferraro</i>	
<b>Cluster analysis for networks using a fuzzy approach</b>	<b>86</b>
<i>Davide Buttarazzi and Giovanni C. Porzio</i>	
<b>Visualizing anomalies in circular data</b>	<b>90</b>
<i>Andrea Cappozzo, Chiara Masci, Francesca Ieva and Anna Maria Paganoni</i>	
<b>Model-based clustering of right-censored lifetime data with frailties and random covariates</b>	<b>91</b>
<i>Michelle Carey and Catherine Higgins</i>	
<b>Clustering imbalanced functional data</b>	<b>95</b>
<i>Alessandro Casa, Thomas Brendan Murphy and Michael Fop</i>	
<b>Partial membership models for high-dimensional spectroscopy data</b>	<b>99</b>

<i>Fabio Centofanti, Antonio Lepore and Biagio Palumbo</i>	
<b>Sparse clustering for functional data</b>	<b>103</b>
<i>Yunxiao Chen, Motonori Oka and Matthias von Davier</i>	
<b>Interpretable and accurate scaling in large-scale assessment: a variable selection approach to latent regression</b>	<b>107</b>
<i>Katharine M. Clark and Paul D. McNicholas</i>	
<b>Clustering three-way data with outliers</b>	<b>111</b>
<i>Roberto Colombi and Sabrina Giordano</i>	
<b>A two-component markov switching regression model</b>	<b>115</b>
<i>Federica Conte and Paola Paci</i>	
<b>The broad phenotype-specific applications of the network-based SWIM tool</b>	<b>119</b>
<i>Houyem Demni, Pierre Miasnikof, Alexander Y. Shestopaloff, Cristián Bravo and Yuri Lawryshyn</i>	
<b>Testing graph clusterability: a density based statistical test for directed graphs</b>	<b>123</b>
<i>Anna Denkowska, Krystian Szczfôśny, Joao Paulo Vieito and Stanisław Wanat</i>	
<b>Deep neural network in the modeling of the dependence structure in risk aggregation</b>	<b>124</b>
<i>Marco Di Marzio, Chiara Passamonti and Charles Taylor</i>	
<b>Circular regression with measurement errors</b>	<b>128</b>
<i>Marco Di Zio, Romina Filippini, Gaia Rocchetti and Simona Toti</i>	
<b>Classification tree to improve data quality in official statistics</b>	<b>132</b>
<i>Rosa Fabbricatore and Maria Iannario</i>	
<b>Uncertainty and response style in latent trait models to assess emotional intelligence of elite swimmers</b>	<b>136</b>
<i>Rosa Fabbricatore, Roberto Di Mari, Zsuzsa Bakk, Mark de Rooij and Francesco Palumbo</i>	
<b>Three-step rectangular latent Markov modeling based on ML correction</b>	<b>140</b>
<i>Alessio Farcomeni, Alfonso Russo and Marco Geraci</i>	
<b>Mid-quantile regression for discrete panel data</b>	<b>144</b>
<i>Matteo Farnè</i>	
<b>Trimmed factorial k-means</b>	<b>148</b>
<i>Florian Felice and Christophe Ley</i>	
<b>Estimation of team's strength for handball games predictions</b>	<b>152</b>
<i>Peter Filzmoser and Marcus Mayrhofer</i>	
<b>Outlier explanation based on Shapley values for vector- and matrix-valued observations</b>	<b>156</b>

<i>Lara Fontanella, Emiliano del Gobbo and Alex Cucco</i>	
<b>Identification of misogynistic accounts on Twitter through Graph Convolutional Networks</b>	<b>159</b>
<i>Giacomo Francisci and Anand Vidyashankar</i>	
<b>Depth functions for tree-indexed processes</b>	<b>163</b>
<i>Carla Galluccio, Matteo Magnani, Davide Vega, Giancarlo Ragozini and Alessandra Petrucci</i>	
<b>Analysing the effect of different design choices in network-based topic detection</b>	<b>164</b>
<i>Luis A. García-Escudero, Christian Hennig, Agustín Mayo-Iscar, Gianluca Morelli and Marco Riani</i>	
<b>A proposal for the joint automated detection of clusters and anomalies</b>	<b>168</b>
<i>V. G. Genova, C. Edling, H. Mondani, A. M. Rostami and M. Tumminello</i>	
<b>Mobility across crimes: statistically validated networks and temporal pattern recognition</b>	<b>172</b>
<i>Paolo Giordani, Susanna Levantesi, Andrea Nigri and Virginia Zarulli</i>	
<b>A cohort study on the gender gap in mortality through the Tucker3 model</b>	<b>176</b>
<i>Luca Greco, Giovanna Menardi and Marco Rudelli</i>	
<b>Trimmed kernel mean shift</b>	<b>180</b>
<i>Bettina Grün, Thomas Petzoldt and Helga Wagner</i>	
<b>Modeling zone diameter measurements to infer antibiotic susceptibility of bacteria</b>	<b>184</b>
<i>Julien Jacques and Francesco Amato</i>	
<b>Clustering longitudinal ordinal data</b>	<b>185</b>
<i>Daniyal Kazempour and Peer Kröger</i>	
<b>“You call it a manifold, I call it a subspace” - selected examples on the interface between computer science and statistics in the context of clustering and manifold learning</b>	<b>187</b>
<i>Annika M. T. U. Kestler, Nensi Ikononi, Silke D. Werle, Julian D. Schwab, Friedhelm Schwenker and Hans A. Kestler</i>	
<b>Sparse rule generating fold-change classification for molecular high-throughput profiles</b>	<b>188</b>
<i>Silvia Komara, Martina Košíková, Erik Šoltés and Tatiana Šoltésová</i>	
<b>Comparison of the households’ work intensity in Slovakia and Czechia through least squares means analysis based on GLM</b>	<b>192</b>
<i>Arnost Komárek</i>	
<b>Model based clustering procedures for multivariate mixed type longitudinal data</b>	<b>193</b>

<i>Tomasz Kwarciński, Paweł Ulman</i>	
<b>Inequality, populism, and unfairness: a comparison of unfair income inequalities in Poland and Norway</b>	<b>196</b>
<i>Francesco Lagona and Marco Mingione</i>	
<b>Segmenting toroidal time series by nonhomogeneous hidden semi-Markov models</b>	<b>197</b>
<i>Roland Langrock and Sina Mews</i>	
<b>How to build your latent Markov model: the role of time and space</b>	<b>201</b>
<i>Paweł Lula, Zsuzsanna Géring, Mńagdalena Talaga, Ildikó Dén-Nagy and Réka Tamássy</i>	
<b>The comparative analysis of publication activity in Hungary and Poland in the field of economics, finance and business</b>	<b>205</b>
<i>Johan Lyrvall, Roberto Di Mari, Zsuzsa Bakk, Jennifer Oser and Jouni Kuha</i>	
<b>An R package for multilevel latent class analysis with covariates</b>	<b>206</b>
<i>R. Neal Mackenzie and Paul D. McNicholas</i>	
<b>Longitudinal hidden Markov models: problems and methods</b>	<b>210</b>
<i>Matteo Magnani, Matias Piqueras, Alexandra Segerberg, Davide Vega and Victoria Yantseva</i>	
<b>Cluster analysis for the study of online visual communication</b>	<b>214</b>
<i>Ichcha Manipur, Ilaria Granata, Lucia Maddalena and Mario R. Guarracino</i>	
<b>Cluster analysis of cancer metabolic network ensembles</b>	<b>218</b>
<i>Carlo Metta, Marco Fantozzi, Andrea Papini, Gianluca Amato, Matteo Bergamaschi, Silvia Giulia Galfrè, Alessandro Marchetti, Michelangelo Vegliò, Maurizio Parton and Francesco Morandin</i>	
<b>Improving performance in neural networks by dendrite-activated connection</b>	<b>219</b>
<i>Rodolfo Metulini, Francesco Biancalani and Giorgio Gnecco</i>	
<b>The Generalized Shapley measure for ranking players in basketball: applications and future directions</b>	<b>223</b>
<i>Rouven Michels, Timo Adam and Marius Ötting</i>	
<b>Tree-based regression within a hidden Markov model framework</b>	<b>227</b>
<i>Boris Mirkin</i>	
<b>Scoring distances between equivalence and preference relations</b>	<b>231</b>
<i>Fabio Morea and Domenico De Stefano</i>	
<b>Evaluation of the performance of a modularity-based consensus community detection algorithm</b>	<b>234</b>

<i>Vincenzo Nardelli and Niccolò Salvini</i>	
<b>Assessing and improving data quality in open spatial data: a case study with ANAC data</b>	<b>238</b>
<i>M. Rosário Oliveira, Diogo Pinheiro and Lina Oliveira</i>	
<b>Visualizing interval Fisher Discriminant Analysis results</b>	<b>239</b>
<i>Niels Lundtorp Olsen, Alessia Pini and Simone Vantini</i>	
<b>Nonparametric local inference for functional data defined on manifold domains</b>	<b>242</b>
<i>Silvia Pandolfi and Francesco Bartolucci</i>	
<b>Case-control variational inference for large scale stochastic block models</b>	<b>246</b>
<i>Francesca Panero</i>	
<b>Issues with sparse spatial random graphs</b>	<b>250</b>
<i>Barbara Pawelek and Maria Sadko</i>	
<b>Corporate bankruptcy prediction: application of statistical learning methods</b>	<b>254</b>
<i>Daniele Pretolesi, Andrea Vian and Annalisa Barla</i>	
<b>Using machine learning and AI in science of science</b>	<b>255</b>
<i>Pascal Pr�ea</i>	
<b>Distances, orders and spaces</b>	<b>259</b>
<i>Antonio Punzo, Luca Bagnato and Salvatore Daniele Tomarchio</i>	
<b>Model-based clustering via parsimonious mixtures of dimension-wise scaled normal mixtures</b>	<b>263</b>
<i>Monia Ranalli and Roberto Rocci</i>	
<b>Model-based simultaneous classification and reduction for three-way ordinal data</b>	<b>264</b>
<i>Jakob Raymaekers and Peter J. Rousseeuw</i>	
<b>The cellwise Minimum Covariance Determinant estimator</b>	<b>268</b>
<i>Maurizio Romano and Roberta Siciliano</i>	
<b>A new accurate heuristic algorithm to solve the rank aggregation problem with a large number of objects</b>	<b>269</b>
<i>Jorge Rueda, Maria del Mar Rueda, Ram�n Ferri and Beatriz Cobo</i>	
<b>Using ML techniques for estimation with non-probabilistic survey data</b>	<b>273</b>
<i>Ana Santos, S�nia Dias, Paula Brito and Paula Amaral</i>	
<b>Multiclass classification of distributional data</b>	<b>276</b>
<i>Lorenzo Schiavon</i>	
<b>Latent Bayesian clustering for topic modelling</b>	<b>280</b>
<i>Michael G. Schimek, Bastian Pfeifer and Marcus D. Bloice</i>	
<b>A novel multi-view ensemble clustering framework for cancer subtype discovery</b>	<b>284</b>



<i>Francesco Schirripa Spagnolo, Gaia Bertarelli, Nicola Salvati, Donato Summa, Monica Scannapieco, Stefano Marchetti and Monica Pratesi</i>	
<b>Reducing selection bias in non-probability sample by Small Area Estimation</b>	<b>288</b>
<i>Pedro Duarte Silva, Peter Filzmoser and Paula Brito</i>	
<b>Sparse and robust estimators for outlier detection in distributional data</b>	<b>292</b>
<i>Andrea Sottosanti, Sara Agavni' Castiglioni, Stefania Pirrotta, Enrica Calura and Davide Risso</i>	
<b>Clustering genes spatial expression profiles with the aid of external biological knowledge</b>	<b>296</b>
<i>Arthur Tenenhaus, Michel Tenenhaus and Theo Dijkstra</i>	
<b>Structural equation modeling with latent/emergent variables: RGCCAc</b>	<b>300</b>
<i>Yoshikazu Terada</i>	
<b>On some properties of reconstructed trajectories from sparse longitudinal data</b>	<b>301</b>
<i>Daniel J.W. Touw, Patrick J.F. Groenen, Ines Wilms and Andreas Alfons</i>	
<b>Clusterpath Gaussian graphical modeling</b>	<b>302</b>
<i>Paweł Ulman, Małgorzata Ćwiek and Maria Sadko</i>	
<b>Housing poverty in Europe. Multidimensional analysis</b>	<b>305</b>
<i>Anand Vidyashankar, Fengnan Deng, Giacomo Francisci and Xiaoran Jiang</i>	
<b>Efficiency and robustness in supervised learning</b>	<b>306</b>
<i>Frédéric Vrins</i>	
<b>Optimal and robust combination of forecasts via constrained optimization and shrinkage</b>	<b>307</b>
<i>Gabriel Wallin, Yunxiao Chen and Irini Moustaki</i>	
<b>DIF analysis with unknown groups and anchor items</b>	<b>308</b>
<i>Felix M. Weidner, Mirko Rossini, Joachim Ankerhold and Hans A. Kestler</i>	
<b>Constraint-based attractor search in Boolean networks using quantum computing</b>	<b>309</b>
<i>Michio Yamamoto and Yoshikazu Terada</i>	
<b>Clustering for sparsely sampled longitudinal data based on basis expansions</b>	<b>312</b>
<i>Naoto Yamashita</i>	
<b>Two extensions of extended redundancy analysis for exploratory data analysis</b>	<b>313</b>
<i>Giorgia Zaccaria</i>	
<b>Ultrametric Gaussian Mixture models with parsimonious structures</b>	<b>314</b>
<i>Li-Chun Zhang</i>	
<b>Using retail transactions for consumer price index and expenditure statistics</b>	<b>318</b>

<b>Contributed Papers</b>	<b>323</b>
<i>Giuseppe Alfonzetti, Luca Grassetti and Laura Rizzi</i>	
<b>Propensity towards Master's degree: choices of northern students after BAs?</b>	<b>325</b>
<i>Giuseppe Alfonzetti, Luca Grassetti and Laura Rizzi</i>	
<b>Classifying northern Italian students in their transition to Master degree</b>	<b>329</b>
<i>Rosa Arboretti, Elena Barzizza, Nicolò Biasetton and Marta Disegna</i>	
<b>Customer satisfaction through time: structured time series from sentiment analysis of TripAdvisor data</b>	<b>333</b>
<i>Roberto Ascari and Alice Giampino</i>	
<b>A flexible topic model</b>	<b>334</b>
<i>Golnoosh Babaei, Paolo Pagnottoni and Thanh Thuy Do</i>	
<b>Explainable machine learning for lending default classification</b>	<b>338</b>
<i>Elena Barzizza, Riccardo Ceccato, Solomon Harrar, Fortunato Pesarin and Luigi Salmaso</i>	
<b>A multivariate permutation test for association</b>	<b>342</b>
<i>Michela Battauz</i>	
<b>A competing risk analysis of academic careers with students' ability and speed as predictors</b>	<b>343</b>
<i>Andriette Bekker, J.T. Ferreira, J. Pillay and M. Arashi</i>	
<b>Bayesian analysis for a graphical t-model</b>	<b>347</b>
<i>Marco Berrettini, Giuliano Galimberti, Thomas Brendan Murphy and Saverio Ranciati</i>	
<b>Modelling soccer players field position via mixture of Gaussians with flexible weights</b>	<b>351</b>
<i>Antonella Bianchino, Daniela Fusco, Paola Giordano, Maria Antonietta Liguori, Maria Carmina Palma and Donato Summa</i>	
<b>Tourism as support in economic development of inner areas: a multi-sources approach</b>	<b>355</b>
<i>Luisa Bisaglia and Francesco Lisi</i>	
<b>SARIMA models with multiple seasonality</b>	<b>358</b>
<i>Stefano Bonnini and Michela Borghesi</i>	
<b>Adoption of 4.0 technologies and related obstacles. Application of a multivariate nonparametric test for categorical variables</b>	<b>362</b>
<i>Giuseppe Bove</i>	
<b>An application of asymmetric multidimensional scaling to the VQR 2015-2019 data</b>	<b>366</b>

<i>Luca Brusa and Fulvia Pennoni</i>	
<b>Improving clustering in temporal networks through an evolutionary algorithm</b>	<b>370</b>
<i>Andrea Carta</i>	
<b>A support vector machine approach to create oblique decision trees for regression</b>	<b>374</b>
<i>Giulia Cereda, Fabio Corradi and Cecilia Viscardi</i>	
<b>Comparing soft classification methods for the rare type match problem</b>	<b>378</b>
<i>Annalisa Cerquetti</i>	
<b>Bayesian Shannon entropy estimation under normalized inverse Gaussian priors via Monte Carlo sampling</b>	<b>382</b>
<i>Lax Chan and Aldo Goia</i>	
<b>Goodness-of-fit test for single functional index model</b>	<b>386</b>
<i>Silvia Columbu, Nicola Piras and Jeroen K. Vermunt</i>	
<b>Multilevel cross-classified latent class models</b>	<b>390</b>
<i>Giulia Contu, Luca Frigau, Marco Ortu and Sara Pau</i>	
<b>Multivariate regression tree to investigate the Italian mortality rates</b>	<b>394</b>
<i>Luca Coraggio and Pietro Coretto</i>	
<b>Empirical analysis of the quadratic scoring for selecting clustering solutions</b>	<b>398</b>
<i>Marcella Corduas and Domenico Piccolo</i>	
<b>Classification of daily streamflow data: a study on regime changes</b>	<b>402</b>
<i>Noemi Corsini and Giovanna Menardi</i>	
<b>Modal clustering for categorical data</b>	<b>406</b>
<i>Cristina Davino, Tormod Næs, Rosaria Romano and Domenico Vistocco</i>	
<b>The use of principal components in quantile regression: a simulation study</b>	<b>410</b>
<i>Antonio De Falco and Antonio Irpino</i>	
<b>An interdisciplinary methodology for socio-economic segregation analysis</b>	<b>414</b>
<i>Houyem Demni and Simona Balzano</i>	
<b>Visualizing classification results: graphical tools for DD-classifiers</b>	<b>418</b>
<i>Claudia Di Caterina</i>	
<b>Detecting the positions of nonconsensus amino acids in HIV patients by marginal likelihood thresholding</b>	<b>419</b>
<i>Davide Di Cecco, Andrea Tancredi and Tiziana Tuoto</i>	
<b>One-inflated Bayesian mixtures for population size estimation</b>	<b>423</b>
<i>Marta Di Lascio and Roberta Pappadà</i>	
<b>Cluster analysis and conditional copula: a joint approach to analyse energy demand</b>	<b>427</b>

<i>Marta Di Lascio, Fabrizio Durante and Aurora Gatto</i>	
<b>Hierarchical percentile clustering to analyse greenhouse gas emissions from agriculture in European Union</b>	<b>431</b>
<i>Cinzia Di Nuzzo and Salvatore Ingrassia</i>	
<b>Maximum likelihood approach to parameter selection in the spectral clustering algorithm</b>	<b>435</b>
<i>José G. Dias</i>	
<b>Finite mixture models: a systematic review</b>	<b>439</b>
<i>Francesco Dotto, Roberto Di Mari, Alessio Farcomeni and Antonio Punzo</i>	
<b>Measurement invariance: a method based on latent Markov models</b>	<b>441</b>
<i>Niccolò Ducci, Leonardo Grilli and Marta Pittavino</i>	
<b>A comparison between the varying-thresholds model and quantile regression</b>	<b>445</b>
<i>Augusto Fasano, Niccolò Anceschi, Beatrice Franzolini and Giovanni Rebaudo</i>	
<b>Efficient computation of predictive probabilities in probit models via expectation propagation</b>	<b>449</b>
<i>Donata Favaro and Anna Giraldo</i>	
<b>How women react to their partners' work instability. The added-worker effect</b>	<b>453</b>
<i>Carlina C. Feldmann, Sina Mews, Rouven Michels and Roland Langrock</i>	
<b>Inference on the state distribution in periodic hidden Markov models</b>	<b>457</b>
<i>Giuseppe Feo, Francesco Giordano, Marcella Niglio, Sara Milito and Maria Lucia Parrella</i>	
<b>Testing clusters of locations in spatial dynamic panel data models</b>	<b>461</b>
<i>Beatrice Franzolini, Laura Bondi, Augusto Fasano and Giovanni Rebaudo</i>	
<b>Bayesian forecasting of multivariate longitudinal zero-inflated counts: an application to civil conflict</b>	<b>465</b>
<i>Francesco Freni and Giovanna Menardi</i>	
<b>Efficient disentangling <math>\gamma</math>-ray sources from diffuse background in the sky map</b>	<b>469</b>
<i>Luca Frigau, Giulia Contu, Marco Ortu and Andrea Carta</i>	
<b>A method to validate clustering partitions</b>	<b>473</b>
<i>Flora Fullone, Gianmarco Farina, Enza Compagnone, Mirella Morrone and Gioacchino de Candia</i>	
<b>Analysis of the need for working timber starting from Istat industrial production data</b>	<b>477</b>
<i>Ravi Kumar Gangadharan, Vanessa Petrarca, Maria Chiara Pagliarella and Giovanni C. Porzio</i>	
<b>Stratified sampling on data nuggets: a strategy for data reduction</b>	<b>481</b>

<i>Ewa Genge</i>	
<b>Is the subjective financial well-being of Polish families changing with time? An empirical study based on constrained latent Markov models</b>	<b>482</b>
<i>Sara Geremia, Fabio Morea and Domenico De Stefano</i>	
<b>Visualization of proximity and role-based embedding in a regional labour flow network</b>	<b>486</b>
<i>Massimiliano Giacalone, Vincenzo Dottorini, Giuseppe Oddo, Vito Santarcangelo and Angelo Romano</i>	
<b>Method for the quality control and operators training in maintenance activities</b>	<b>490</b>
<i>Lorenzo Giammei, Flaminia Musella, Fulvia Mecatti and Paola Vicard</i>	
<b>Building improved gender equality composite indicators by object-oriented Bayesian networks</b>	<b>494</b>
<i>Sabrina Giordano, Roberta Varriale and Mariangela Zenga</i>	
<b>A comparative study of financial literacy using data from PISA survey</b>	<b>498</b>
<i>Natalia Golini, Francesca Martella and Antonello Maruotti</i>	
<b>On model-based clustering for equitable and sustainable well-being at local level: how many Italies?</b>	<b>499</b>
<i>Luca Greco, Antonio Lucadamo and Claudio Agostinelli</i>	
<b>Model-based clustering for torus data</b>	<b>503</b>
<i>Giulio Grossi and Emilia Rocco</i>	
<b>AutoSynth index: a synthetic indicator for socio-economic development based on autoencoders</b>	<b>507</b>
<i>Lucia Guastadisegni, Irini Moustaki, Silvia Cagnone and Vassilis Vasdekis</i>	
<b>A statistical test to assess the non-normality of the latent variable distribution</b>	<b>511</b>
<i>Christian Hennig and Keefe Murphy</i>	
<b>Quantifying variable importance in cluster analysis</b>	<b>515</b>
<i>Mia Hubert, Iwein Vranckx, Jakob Raymaekers, Bart De Ketelaere and Peter Rousseeuw</i>	
<b>Real-time discriminant analysis in the presence of label and measurement noise</b>	<b>519</b>
<i>Carmela Iorio, Giuseppe Pandolfo and Antonio D'Ambrosio</i>	
<b>A proposal to evaluate the solution of a fuzzy clustering algorithm</b>	<b>520</b>
<i>Aazm Kheyri, Andriette Bekker and Mohammad Arashi</i>	
<b>A fused-type elastic net Gaussian graphical model for paired data</b>	<b>524</b>
<i>Amir Khorrami Chokami</i>	
<b>Complete records over independent FGM sequences</b>	<b>528</b>

<i>Ursula Laa and Dianne Cook</i>	
<b>New tour methods for visualizing high-dimensional data</b>	<b>532</b>
<i>Michele Lambardi di San Miniato, Michela Battauz, Ruggero Bellio and Paolo Vidoni</i>	
<b>Bayesian aggregation of crowd judgments for quantitative fact checking</b>	<b>536</b>
<i>Salvatore Latora and Luigi Augugliaro</i>	
<b>Supervised classification of curves by functional data analysis: an application to neuromarketing data</b>	<b>540</b>
<i>Gertraud Malsiner-Walli, Bettina Grün and Sylvia Frühwirth-Schnatter</i>	
<b>Capturing correlated clusters using mixtures of latent class models</b>	<b>544</b>
<i>Laura Marcis, Maria Chiara Pagliarella and Renato Salvatore</i>	
<b>A three-way “indirect” redundancy analysis</b>	<b>545</b>
<i>Maria Francesca Marino, Matteo Sani and Monia Lupporelli</i>	
<b>Multi-level stochastic blockmodels for multiplex networks</b>	<b>549</b>
<i>Francesca Martella, Xiaoke Qin, Wangshu Tu and Sanjena Subedi</i>	
<b>The multivariate cluster-weighted disjoint factor analyzers model</b>	<b>553</b>
<i>Raffaele Mattera, Germana Scepi, Pooria Ebrahimi and Fabio Matano</i>	
<b>Spatial modelling of pyroclastic cover deposit thickness with remote sensing data and ground measurements: a forecasting combination approach</b>	<b>557</b>
<i>Fiammetta Menchetti</i>	
<b>Granger network on Santa Maria del Fiore Dome</b>	<b>561</b>
<i>Giuseppe Mignemi, Ioanna Manolopoulou and Antonio Calcagni</i>	
<b>Group’s heterogeneity in rating tasks: a Bayesian semi-parametric approach</b>	<b>565</b>
<i>Dung Ngoc Nguyen and Alberto Roverato</i>	
<b>Lattice of Gaussian graphical models for paired data with common undirected structure</b>	<b>569</b>
<i>Marco Ortu, Giulia Contu and Luca Frigau</i>	
<b>Multivariate regression tree topic modeling</b>	<b>573</b>
<i>Lucio Palazzo, Alfonso Iodice D’Enza, Francesco Palumbo and Domenico Vistocco</i>	
<b>Dendrogram slicing through a permutation test approach reconsidered</b>	<b>577</b>
<i>Roberta Paroli and Luigi Spezia</i>	
<b>Markov switching autoregressive models for the analysis of hydrological time series</b>	<b>581</b>
<i>Davide Passaro, Luca Tardella, Giovanna Jona Lasinio, Tiziana Fragasso, Valeria Raggi and Zaccaria Ricci</i>	
<b>A case study of electronic medical records use for predicting kidney injury</b>	<b>585</b>

<i>Matteo Pedone, Raffaele Argiento and Francesco C. Stingo</i>	
<b>Personalized treatment selection model for survival outcomes</b>	<b>589</b>
<i>Danilo Petti, Marcella Niglio and Marialuisa Restaino</i>	
<b>Variable ranking in bivariate copula survival models</b>	<b>593</b>
<i>Pia Pfeiffer and Peter Filzmoser</i>	
<b>Robust penalized multivariate analysis for high-dimensional data</b>	<b>597</b>
<i>Francesco Porro</i>	
<b>Structural zeros in regression models with compositional explanatory variables</b>	<b>600</b>
<i>Kemmawadee Preedalikit, Daniel Fernández, Ivy Liu, Louise McMillan, Marta Nai Ruscone and Roy Costilla</i>	
<b>One-dimensional mixture-based clustering for ordinal responses</b>	<b>604</b>
<i>Iuliia Promskaia, Adrian O'Hagan and Michael Fop</i>	
<b>A compositional stochastic block model for the analysis of the Erasmus programme network</b>	<b>608</b>
<i>Claudia Rampichini and Maria Brigida Ferraro</i>	
<b>A proposal of deep fuzzy clustering by means of the simultaneous approach</b>	<b>609</b>
<i>Maria Giovanna Ranalli, Fulvia Pennoni, Francesco Bartolucci and Antonietta Mira</i>	
<b>When nonresponse makes estimates from a census a small area estimation problem: the case of the survey on Graduates' Employment Status in Italy</b>	<b>613</b>
<i>Edoardo Redivo and Cinzia Viroli</i>	
<b>A supervised classification strategy based on the novel directional distribution depth function</b>	<b>617</b>
<i>Ilaria Rocco</i>	
<b>An application of CART algorithm to administrative data: analysis of youth initial employment trajectories</b>	<b>621</b>
<i>Dorota Rozmus</i>	
<b>Resampling for stability estimation vs. cluster validation via data splitting and subsampling. Which approach is better in detection of clusters in taxonomy?</b>	<b>625</b>
<i>Annalina Sarra, Adelia Evangelista, Tonio Di Battista, and Sergio Palermi</i>	
<b>Functional data analysis approach for identifying redundancy in air quality monitoring stations</b>	<b>627</b>
<i>Luca Scaffidi Domianello</i>	
<b>Student mobility in higher education: a destination-specific local analysis</b>	<b>631</b>
<i>Rosaria Simone</i>	
<b>Residuals diagnostics for model-based trees for ordered rating responses</b>	<b>635</b>

<i>Alexa Sochaniwsky and Paul D. McNicholas</i>	
<b>Hidden Markov models for multivariate longitudinal data</b>	<b>639</b>
<i>Andrzej Sokołowski, Małgorzata Markowska and Maciej Laburda</i>	
<b>K-means clustering - new variations</b>	<b>643</b>
<i>Daniele Spinelli, Salvatore Ingrassia and Giorgio Vittadini</i>	
<b>A Stata implementation of cluster weighted models: the CWMGLM package</b>	<b>644</b>
<i>Salvatore D. Tomarchio, Antonio Punzo and Antonello Maruotti</i>	
<b>Matrix-variate hidden Markov regressions</b>	<b>648</b>
<i>Cristian Usala, Isabella Sulis and Mariano Porcu</i>	
<b>Inequalities at entrance, labour market conditions and university dropout: first evidence from Italy</b>	<b>652</b>
<i>Rosanna Verde, Gianmarco Borrata and Antonio Balzanella</i>	
<b>A clustering method for distributional data based on a LDQ transformation</b>	<b>656</b>
<i>Helga Wagner and Roman Pfeiler</i>	
<b>Shrinkage of time-varying effects in panel data models</b>	<b>657</b>
<i>Carlo Zaccardi, Pasquale Valentini and Luigi Ippoliti</i>	
<b>A Bayesian spatio-temporal regression approach for confounding adjustment</b>	<b>661</b>
<i>Gianpaolo Zammarchi</i>	
<b>Linear random forest to predict energy consumption</b>	<b>665</b>



## Preface

This book collects the abstracts and short papers presented at CLADAG 2023, the 14th Scientific Meeting of the Classification and Data Analysis Group (CLADAG) of the Italian Statistical Society (SIS). The meeting has been organized by the Department of Economics and Statistics of the University of Salerno, under the auspices of the University of Salerno, the SIS and the International Federation of Classification Societies (IFCS).

CLADAG is a member of the IFCS, a federation of national, regional, and linguistically-based classification societies. It is a non-profit, non-political scientific organization, whose aims are to further classification research. Every two years, CLADAG organizes a scientific meeting, devoted to the presentation of theoretical and applied papers on classification and related methods of data analysis in the broad sense. This includes advanced methodological research in multivariate statistics, mathematical and statistical investigations, survey papers on the state of the art, real case studies, papers on numerical and algorithmic aspects, applications in special fields of interest, and the interface between classification and data science. The conference aims at encouraging the interchange of ideas in the above-mentioned fields of research, as well as the dissemination of new findings. CLADAG conferences, initiated in 1997 in Pescara (Italy), were soon considered as an attractive information exchange market and became an important meeting point for people interested in classification and data analysis. A selection of the presented papers is regularly published in (post-conference) proceedings, typically by Springer Verlag.

The Scientific Committee of CLADAG 2023 conceived the Keynote Sessions to provide a fresh perspective on the state of the art of knowledge and research in the field. The scientific program of CLADAG 2023 is particularly rich. All in all, it comprises 5 Keynote Lectures, 31 Invited Sessions promoted by the members of the Scientific Program Committee, and 27 Contributed Sessions. We thank all the session organizers for inviting renowned speakers, coming from many different countries. We are greatly indebted to the referees, for the time spent in a careful review of the abstracts and short papers collected in this book. Special thanks are finally due to the members of the Local Organizing Committee and all the people who collaborated for CLADAG 2023. Last but not least, we thank all the authors and participants, without whom the conference would not have been possible.

Pietro Coretto  
Giuseppe Giordano  
Michele La Rocca  
Maria Lucia Parrella  
Carla Rampichini

Salerno, September 2023



# A THREE-WAY “INDIRECT” REDUNDANCY ANALYSIS

Laura Marcis<sup>1</sup>, Maria Chiara Pagliarella<sup>1</sup> and Renato Salvatore<sup>1</sup>

<sup>1</sup> Department of Economics and Law, University of Cassino and Southern Lazio, (e-mail: [laura.marcis@unicas.it](mailto:laura.marcis@unicas.it), [mc.pagliarella@unicas.it](mailto:mc.pagliarella@unicas.it), [rsalvatore@unicas.it](mailto:rsalvatore@unicas.it))

**ABSTRACT:** This work introduces a composite Three-Way application of the High Order Singular Value Decomposition. Two of the three component data matrices are processed by a standard Redundancy Analysis. The remaining “external” data matrix is related to the others in a heterogeneous system of relations, that can be well suited to tensor analysis. The external data are set to be linked with the first matrix, while with the second matrix the relations are explained only through multivariate linear regression. An application introduces the method, based on the official data from the Italian Equitable and Sustainable Well-being indicators.

**KEYWORDS:** Tucker decomposition, high order singular value decomposition, redundancy analysis.

## 1 Introduction and background

Tensor decomposition (Kolda & Bader, 2009) has the main objective of reducing complex information detected by higher dimensional arrays of data. From a pure statistical perspective, there are two important exploitations of the tensor analysis: the Candecomp/Parafac decomposition and the Tucker decomposition. They play the role of the extension to tensor objects of the principal component analysis (PCa), recognized as an explorative way to approach multidimensional information (Kroonenberg, 2008). In the literature, the most popular tensor decompositions are “Canonical Decomposition” and the “High Order SVD” (HOSVD, De Lathauwer *et al.*, 2000). The HOSVD decomposes an N-mode tensor, as a multidimensional array, in a core reduced-order tensor, multiplied by component matrices alongside each of the N modes. Three-way PCa was the first extension of the PCa to a three-way data set, giving the first useful employment of tensor analysis to explorative statistical analysis. In standard PCa, the components that come from the SVD that summarize individuals are uniquely related to the components that summarize variables. In a three-way PCa the components that summarize entities in each of the modes are related with the remaining two. Redundancy Analysis (RDA, Legendre

and Legendre, 2012) was originally introduced in order to capture the effect onto a reduced space  $\widehat{\mathbf{Y}}_X = \mathbf{X}\widehat{\mathbf{B}}$  of the linear dependence by a set of criterion variables  $\mathbf{Y}$  from a set of predictors  $\mathbf{X}$ , where  $\widehat{\mathbf{B}}$  is the matrix of the ordinary least squares multivariate regression estimates. RDA provides a constrained analysis of the whole linear relations between the two sets of variables, and an unconstrained analysis given by the set of multivariate regression residuals. It can be considered as an extension of multivariate regression because models the effects of the explanatory variables on a response matrix. Partial RDA (pRDA) explores the effects of the predictors in  $\mathbf{X}$  on the  $\mathbf{Y}$  variables, given the covariates of some additional exploratory variables in a matrix  $\mathbf{Z}$ . It is a standard RDA performed taking into account the  $\mathbf{X}$  variables as predictors on  $\mathbf{Y} - \widehat{\mathbf{Y}}_Z$ , with the “effect” by  $\mathbf{Z}$  removed. Nevertheless, the relations between the variables  $\mathbf{Y}$  and  $\mathbf{Z}$  may be quite several. While remaining the same the role of the predictors  $\mathbf{X}$  on  $\mathbf{Y}$ , a third set of variables  $\mathbf{Z}$  may be related and depend on  $\mathbf{Y}$ , by an existing but not well defined dependence. Thus, applying multivariate regression may result hardly appropriate. Variables in  $\mathbf{Z}$  in some cases can not be modeled on  $\mathbf{Y}$  as predictors in a multivariate regression, while  $\mathbf{X}$  predict  $\mathbf{Y}$  and, indirectly through  $\mathbf{Y}$ , the variables in  $\mathbf{Z}$ . Residuals  $\mathbf{Y} - \widehat{\mathbf{Y}}_X$  may take in account the role of  $\mathbf{X}$  in the “indirect” explanation of  $\mathbf{Z}$ . This is somewhat different from pRDA, because  $\mathbf{Y}$  is not regressed on  $\mathbf{Z}$ , as the external set of covariates from which we remove the effect on  $\mathbf{Y}$ , and also  $\mathbf{Z}$  is not related with  $\mathbf{Y}$  through linear regression. Given a 3rd-order tensor  $\mathcal{X} \in \mathbb{R}^{I \times J \times K}$ , the Tucker decomposition through the HOSVD decomposes the tensor  $\mathcal{X}$  into a core tensor  $\mathcal{G}$  and factor matrices along each mode, as follows:

$$\mathcal{X} \approx \mathcal{G} \times_1 \mathbf{A} \times_2 \mathbf{B} \times_3 \mathbf{C}$$

with the correspondent elementwise expression  $x_{ijk} = \sum_{r=1}^R \sum_{s=1}^S \sum_{t=1}^T g_{rst} a_{ir} b_{js} c_{kt}$ , with  $i = 1, \dots, I, j = 1, \dots, J, k = 1, \dots, K$ . The factor matrices are columnwise orthonormal,  $\mathbf{A} = [\mathbf{a}_1, \dots, \mathbf{a}_R]$ ,  $\mathbf{B} = [\mathbf{b}_1, \dots, \mathbf{b}_S]$ ,  $\mathbf{C} = [\mathbf{c}_1, \dots, \mathbf{c}_T]$ , with  $r = 1, \dots, R, s = 1, \dots, S, t = 1, \dots, T$ . The matricized forms, one per mode, of the 3-way tensor  $\mathcal{X}$  are:

$$\begin{aligned} \mathbf{X}_{(1)} &\approx \mathbf{A}(\mathbf{C} \odot \mathbf{B})' = \mathbf{A}\mathbf{G}_{(1)}(\mathbf{C} \otimes \mathbf{B})', \\ \mathbf{X}_{(2)} &\approx \mathbf{B}(\mathbf{C} \odot \mathbf{A})' = \mathbf{B}\mathbf{G}_{(2)}(\mathbf{C} \otimes \mathbf{A})', \\ \mathbf{X}_{(3)} &\approx \mathbf{C}(\mathbf{B} \odot \mathbf{A})' = \mathbf{C}\mathbf{G}_{(3)}(\mathbf{B} \otimes \mathbf{A})', \end{aligned}$$

with the symbols  $\odot$  and  $\otimes$  that are the Khatri-Rao and Kronecker products, respectively. If  $r_R(\mathcal{X})$  is the rank of the tensor  $\mathcal{X}$  alongside one of the modes,

**Table 1.** Description of the variables used for the application

Variables	Description
S8	Age-standardised mortality rate for dementia and nervous system diseases
IF3	People having completed tertiary education (30-34 years old)
L12	Share of employed persons who feel satisfied with their work
REL4	Social participation
POL5	Trust in other institutions like the police and the fire brigade
SIC1	Homicide rate
BS3	Positive judgement for future perspectives
PATR9	Presence of Historic Parks/Gardens and other Urban Parks recognised of significant public interest
AMB9	Satisfaction for the environment - air, water, noise
INN1	Percentage of R&D expenditure on GDP
Q2	Children who benefited of early childhood services
BE1	Per capita adjusted disposable income
LBE1	Logarithm of Per capita adjusted disposable income

the HOSVD may uses Alternating Least Squares, in order to find:

$$\min_{\mathcal{G}, \mathbf{A}, \mathbf{B}, \mathbf{C}} \|\mathcal{X} - \mathcal{G} \times_1 \mathbf{A} \times_2 \mathbf{B} \times_3 \mathbf{C}\|.$$

Making the substitutions  $\mathbf{A} = \mathbf{Y}$ ,  $\mathbf{B} = \mathbf{Y} - \widehat{\mathbf{Y}}_X$ ,  $\mathbf{C} = \mathbf{Z}$ , with  $I = J = K = n$ ,  $R = S = r(\mathbf{Y}) = r(\mathbf{Y} - \widehat{\mathbf{Y}}_X)$ , and  $T = r(\mathbf{Z})$ , we achieve the desired result, by finding a Three-Way version of the "indirect" RDA, with the proper data matrices. Like in the standard RDA, the data in  $\mathbf{Y}$ ,  $\mathbf{X}$ , and  $\mathbf{Z}$  have to be preprocessed by centering and standardizing their column vectors. This is requested before the application of the RDA of  $\mathbf{Y}$  on  $\mathbf{X}$ .

## 2 Application study

The Equitable and Sustainable Well-being indicators (BES) are designed to define the economic policies which largely act on some fundamental aspects of the quality of life. Table 2 reports the description of these indicators. We use the latter as the predictor variable in the RDA that gives the constrained analysis in the subspace of  $\widehat{\mathbf{Y}}_X$ . Table 2 reports the correlation matrix between the column vectors of  $\mathbf{Y}$ ,  $\mathbf{Y}^*$ , and  $\mathbf{Z}$ . Correlations in bold are significant. It is interesting to remark that in some cases the variables in  $\mathbf{Z}$  are correlated with the columns of  $\mathbf{Y}$ , while they are generally poorly related with the RDA residuals vectors (given by the unconstrained RDA). In particular, the evidence is that even if  $\mathbf{Z}$  may be regressed on  $\mathbf{Y}$ , for some variables the regression on  $\mathbf{X}$  results inappropriate. One of the important cases is shown by the variable AMB9. This variable (Satisfaction for the environment - air, water, noise) is permanently correlated with the variable BS3 (Positive judgement for future

**Table 2.** Correlations - Matrices  $\mathbf{Y}$ ,  $\mathbf{Y}^*$ , and  $\mathbf{Z}$

Variable	$Y1_{BS3}$	$Y2_{INN1}$	$Y3_{IF3}$	$Y4_{O2}$	$Y5_{L12}$	$Y6_{S8}$
$Z1_{AMB9}$	<b>0,4029</b>	-0,0239	<b>0,4570</b>	<b>0,6852</b>	<b>0,8090</b>	<b>0,6926</b>
$Z2_{POL5}$	0,1906	<b>0,3629</b>	<b>0,2594</b>	<b>0,6395</b>	<b>0,6330</b>	<b>0,5973</b>
$Z3_{PATR9}$	0,1800	<b>0,3759</b>	0,0426	0,0353	0,0146	<b>0,2420</b>
$Z4_{RELA}$	<b>0,5133</b>	<b>0,2601</b>	<b>0,4413</b>	<b>0,7026</b>	<b>0,8380</b>	<b>0,6507</b>
$Z5_{SIC1}$	<b>-0,2215</b>	-0,1150	<b>-0,4665</b>	<b>-0,5397</b>	<b>-0,5925</b>	<b>-0,6343</b>
Variable	$Y1^*_{BS3}$	$Y2^*_{INN1}$	$Y3^*_{IF3}$	$Y4^*_{O2}$	$Y5^*_{L12}$	$Y6^*_{S8}$
$Z1_{AMB9}$	<b>0,4605</b>	-0,1075	<b>0,2848</b>	0,1294	0,0423	-0,0119
$Z2_{POL5}$	0,0042	-0,1972	-0,0523	0,0662	-0,0624	-0,0755
$Z3_{PATR9}$	-0,1311	0,2081	<b>-0,2749</b>	<b>0,2794</b>	0,0053	0,1774
$Z4_{RELA}$	<b>0,3595</b>	-0,0025	-0,0056	0,0993	-0,1227	-0,1229
$Z5_{SIC1}$	-0,2029	-0,0184	<b>-0,3021</b>	-0,1787	-0,0291	-0,0234

perspectives), whatever is  $\mathbf{y}$  or  $\mathbf{y}^* = \mathbf{y} - \widehat{\mathbf{y}}_X$  (with  $corr(\mathbf{y}, \mathbf{y}^*) = 0.7293$ ). We have a moderate correlation between the variable BS3 and the correspondent RDA residuals, and a moderate explanation of this variable is given by the BE1 (Per capita adjusted disposable income). Then, a tentative conclusion is that the “Satisfaction for the environment” (a  $\mathbf{Z}$  variable) does not depend on the “Disposable income” (the RDA predictor  $\mathbf{X}$ ). An opposite case occurs when we try to assess the same AMB9 variable, versus L12 (Share of employed persons who feel satisfied with their work). Even we have that  $corr(\mathbf{y}, \mathbf{y}^*) = -0.2395$ , AMB9 has the greatest correlation with the observed L12 ( $\mathbf{y}$ ), which reduces to be not significant in terms of L12 RDA residuals ( $\mathbf{y}^*$ ). Thus, even the “Share of employed persons who feel satisfied with their work” depends on the “Disposable income”, and the “Satisfaction for the environment” can be explained by the relation with “People that feel satisfied with their work”, the “Satisfaction for the environment” depends on the “Disposable income” through its relation with the “People that feel satisfied with their work”.

## References

- DE LATHAUWER, LIEVEN, DE MOOR, BART, & VANDEWALLE, JOOS. 2000. A multilinear singular value decomposition. *SIAM journal on Matrix Analysis and Applications*, **21**(4), 1253–1278.
- KOLDA, TAMARA G, & BADER, BRETT W. 2009. Tensor decompositions and applications. *SIAM review*, **51**(3), 455–500.
- KROONENBERG, PIETER M. 2008. *Applied multiway data analysis*. John Wiley & Sons.
- LEGENDRE, PIERRE, & LEGENDRE, LOUIS. 2012. *Numerical ecology*. Elsevier.